# Homework 3 – Conditional Probability

# Admissions Data

Consider the following dataset with 4486 college admission decisions in a frequency table with program, gender, and decision fields. Assume each person only applies to one program.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Program | Male (M) | | Female (F) | |
| Accepted (A) | Denied (D) | Accepted (A) | Denied (D) |
| P1 | 512 | 313 | 89 | 19 |
| P2 | 313 | 207 | 17 | 8 |
| P3 | 120 | 205 | 202 | 391 |
| P4 | 138 | 279 | 131 | 244 |
| P5 | 53 | 138 | 94 | 299 |
| P6 | 22 | 351 | 24 | 317 |

Compute the following probabilities:

* + 1. Marginal probability of being accepted *P* (*A*)
       - * P = 0.382 or
    2. Marginal probability of applying to program P1 *P* (*P* 1)
       - * P = 0.207 or
    3. Union probability of applying to either program P1 or P2 *P* (*P* 1 *∪ P* 2)
       - * P = 0.329 or
    4. Joint probability of applying to program P1 and being male *P* (*P* 1 *∩ M)*
       - * P = 0.184 or
    5. Joint probability of applying to program P1 being accepted *P* (*P* 1 *∩ A*)
       - * P = 0.134 or
    6. Conditional probability of acceptance for females’ *P* (*A|F)* and males’ *P* (*A|M)*
       - * P (A|F) = 0.303 or
         * P (A|M) = 0.436 or
    7. Conditional probability of acceptance for females and males in each program:
       1. ***P* (*A|F, P* 1) and *P* (*A|M, P* 1)**
          - P (A|F, P1) = 0.824 or
          - P (A|M, P1) = 0.620 or
       2. ***P* (*A|F, P* 2) and *P* (*A|M, P* 2)**
          - P (A|F, P2) = 0.68 or
          - P (A|M, P2) = 0.601 or
       3. ***P* (*A|F, P* 3) and *P* (*A|M, P* 3)**
          - P (A|F, P3) = 0.34 or
          - P (A|M, P3) = 0.369 or
       4. ***P* (*A|F, P* 4) and *P* (*A|M, P* 4)**
          - *P (A|F, P4) = 0.349 or*
          - *P (A|M, P4) = 0.33 or*
       5. ***P* (*A|F, P* 5) and *P* (*A|M, P* 5)**
          - P (A|F, P3) = 0.239 or
          - P (A|M, P3) = 0.277 or
       6. ***P* (*A|F, P* 6) and *P* (*A|M, P* 6)**
          - P (A|F, P3) = 0.058 or
          - P (A|M, P3) = 0.07 or
    8. **Based on results of (f) and (g) above, do gender and acceptance appear to be independent? Why may this result be important for an admissions committee?**

Yes, the gender and acceptance appear to be independent. The percentage of Male and Female in acceptance is nearly the same. Having this result shows that there is no gender bias in selection. Assuming that acceptance is calculated on merit and not just for maintaining negligible gender bias.

# Rock, Paper, Scissors

**Play *N* = 30 rounds of “Rock-Paper-Scissors” and record the results of each game (*Xi*: your move and *Yi*: your opponent’s move). Record your results in a 3 x 3 frequency table similar to the one below.**

**Note: you can play against a computer here:** [**http://www.nytimes.com/interactive/science/rock-paper-scissors.html**](http://www.nytimes.com/interactive/science/rock-paper-scissors.html)

|  |  |  |  |
| --- | --- | --- | --- |
| Your Move (Xi) | Opponent’s Move (Yi) | | |
| Rock (YR) | Paper (YP ) | Scissors (YS) |
| Rock (XR) | 2 | 3 | 4 |
| Paper (XP ) | 6 | 3 | 4 |
| Scissors (XS) | 2 | 3 | 3 |

* + 1. Compute the marginal probability of each opponent’s move: *P* (*YR*)*, P* (*YP* )*, P* (*YS*).
       - * P (Yr) = 0.3
         * P(Yp) = 0.3
         * P(Ys) = 0.3
    2. Write a mathematical expression using joint and union operators for and compute the probability of you winning a game.
    3. Write a mathematical expression using joint and union operators for and compute the probability of tie game.